

Summary of Factoring Techniques



Factoring the Greatest Common Factor from a Polynomial

Example:	$24a^3b^2 - 4a^2b^2 - 16a^2b^4$ $= 4a^2b^2(6a - 1 - 4b^2)$	<ol style="list-style-type: none"> 1. Find the G.C.F of all terms. G.C.F = $4a^2b^2$ 2. Factor the GCF from each term of the polynomial.
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Factoring by Grouping

Example #1	$3(x + y) + a(x + y)$ $= (x + y)(3 + a)$	<ol style="list-style-type: none"> 1. Both terms have a factor of $(x + y)$. 2. Factor out $(x + y)$ from each term.
Example #2	$a^2b + 3a^2 + 2b + 6$ $= \underline{a^2b + 3a^2} + \underline{2b + 6}$ $= a^2(b + 3) + 2(b + 3)$ $= (b + 3)(a^2 + 2)$	<ol style="list-style-type: none"> 1. Group with parentheses the 1st two terms and the last two terms. 2. Factor out the GCF from each group. Notice: Both terms have a factor of $(b + 3)$. 3. Factor out $(b + 3)$ from each term.

Factoring a Trinomial of the Form $x^2 + bx + c$ (Leading coefficient is 1)

Example #1	$x^2 + 12x + 20$ Factors of 20: $\left\{ \begin{array}{l} 1 \cdot 20 \rightarrow 1 + 20 = 21 \\ 2 \cdot 10 \rightarrow 2 + 10 = 12 \leftarrow 2 \text{ and } 10!!!! \\ 4 \cdot 5 \rightarrow 4 + 5 = 9 \end{array} \right.$ $= (x + 2)(x + 10)$	<ol style="list-style-type: none"> 1. What 2 numbers: MULTIPLY to = 20 and ADD to = 12 ??? 2. List the factors of 20 and check the sums. 3. Factor.
Example #2	$x^2 - 15x + 56$ Factors of 56: $\left\{ \begin{array}{l} (-1)(-56) \rightarrow \\ (-2)(-28) \rightarrow \\ (-4)(-14) \rightarrow \\ (-7)(-8) \rightarrow (-7) + (-8) = -15 \leftarrow -7 \text{ and } -8!!!! \end{array} \right.$ $= (x - 7)(x - 8)$	<ol style="list-style-type: none"> 1. What 2 numbers: MULTIPLY to = 56 and ADD to = -15 ??? 2. List the factors of 56 and check the sums. 3. Factor.
Example #3	$x^2 + 2x - 35$ $7 \cdot (-5) = -35, \text{ and } 7 + (-5) = 2 \leftarrow \text{The numbers are } 7 \text{ and } -5.$ $= (x + 7)(x - 5)$	Steps 1, 2, 3 from above.

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Factoring a Trinomial of the Form $ax^2 + bx + c$, $a \neq 1$ (Leading coefficient is not 1)

Method #1: The "AC" method

Example: $2x^2 + 7x - 4$

$$(8)(-1) = -8, \text{ and } 8 + (-1) = 7$$

$$= 2x^2 - 1x + 8x - 4$$

$$= 2x^2 - 1x + \frac{8x - 4}{1}$$

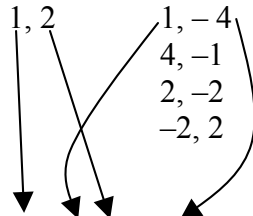
$$= x(2x - 1) + 4(2x - 1)$$

$$= (2x - 1)(x + 4)$$

1. Multiply 2 and $-4 = -8$.
2. What 2 numbers: MULTIPLY to $= -8$ and ADD to $= 7$???
The numbers are 8 and -1 .
3. Split up the $7x$ term $\rightarrow -1x + 8x$
4. Group the 1st 2 terms and the last 2 terms.
5. Factor out the GCF from each group.
6. Factor out the common factor of $(2x - 1)$.

Method #2: Factoring by "Trial and Error"

Example: $2x^2 + 7x - 4$



$$(1x + 1)(2x - 4) = 2x^2 - 4x + 2x - 4 \neq \text{original polynomial}$$

$$(1x - 1)(2x + 4) = 2x^2 + 4x - 2x - 4 \neq \text{original polynomial}$$

$$(x + 4)(2x - 1) = 2x^2 - 1x + 8x - 4 = 2x^2 + 7x - 4$$

and so on...

$$= (x + 4)(2x - 1) \text{ is the correct factorization.}$$

1. Constant term is negative
2. List factors of 2 and -4 .
3. Create TRIAL factors and FOIL out to pick the CORRECT factorization.

Special Factoring

Difference of 2 squares: $A^2 - B^2 = (A - B)(A + B)$

Example: $x^2 - 49$

$$= x^2 - 7^2$$

$$= (x - 7)(x + 7)$$

1. Let $A = x$, $B = 7$
2. Factor using the rule of difference of squares.

Perfect Square trinomial: $A^2 + 2AB + B^2 = (A + B)(A + B) = (A + B)^2$

$$A^2 - 2AB + B^2 = (A - B)(A - B) = (A - B)^2$$

Example: $x^2 - 10x + 25$

$$= x^2 - 2 \cdot 5 \cdot x + 5^2$$

$$= (x - 5)(x - 5) = (x - 5)^2$$

1. Let $A = x$, $B = 5$
2. Factor using the rule of perfect sq. trinomial.

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